## **Abstract**

Differential operators on affine algebraic varieties were defined by A.Grothendieck. They contain, in particular, the rings of polynomial functions on the varieties and all their derivations. The latter are a rich source of simple infinite dimensional Lie algebras. We will discuss the state of the art of the representation theory of these Lie algebras.