

## Abstract

Given integers  $k_1, k_2$  with  $0 \leq k_1 < k_2$ , the determinations of all positive integers  $q$  for which there exists a perfect Splitter  $B[-k_1, k_2](q)$  set is a wide open question in general. In this paper, we obtain new necessary and sufficient conditions for an odd prime  $p$  such that there exists a nonsingular perfect  $B[-1, 3](p)$  set. We also give some necessary conditions for the existence of purely singular perfect splitter sets. In particular, we determine all perfect  $B[-k_1, k_2](2^n)$  sets for any positive integers  $k_1, k_2$  with  $k_1 < k_2 \leq 4$ ; we show that if  $k, n$  are positive integers with  $k \geq 2$  and there exists a perfect  $B[-k, k](n)$  set, then  $n = 2k$ . We also prove that there are infinitely many prime  $p$  such that there exists a perfect  $B[-1, 3](p)$  set.