Abstract

We study the regularity of the conjugacy between an irreducible Anosov automorphism \$A\$ on torus and its small perturbation \$f\$.

We say that \$f\$ and \$A\$ have the same periodic data if the derivatives of the return maps of \$f\$ and \$A\$ at the corresponding periodic points are conjugate. It is conjectured that \$f\$ is \$C^\infty\$ conjugate to \$A\$ if and only if \$f\$ and \$A\$ have the same periodic data. In this paper, we confirm the conjecture.

This completes the characterization of the most elementary \$C^1\$-invariant for local \$C^\infty\$ rigidity.

We also give the first example of cocycle rigidity over fibers with conjugate periodic data.