

## Abstract

Let  $C$  be an  $[n, k]$  linear code over the finite field  $F_q$ . Let  $d_i(C)$  denote its insertion-deletion (insdel for short) distance, which characterizes the insdel error-correcting capability of  $C$ . In this paper we propose a strict half-Singleton upper bound  $d_i(C) \leq 2(n-2k+1)$  if  $C$  does not contain the codeword with all 1s, which generalizes the half-Singleton bound on the insdel distances of linear codes due to Cheng-Guruswami-Haeupler-Li, and a stronger direct upper bound  $d_i(C) \leq 2(d_H(C)-t)$  under a weak condition, where  $t \geq 1$  is a positive integer determined by the generator matrix and  $d_H(C)$  denotes the Hamming distance of  $C$ . A sufficient condition for a linear code attaining the strict half-Singleton bound is given. We prove that the code length of an optimal binary linear insdel code with respect to the (strict) half-Singleton bound is about twice its dimension and conjecture that optimal binary linear insdel codes have exact parameters  $[2k, k, 4]$  or  $[2k+1, k, 4]$  with respect to the half- or strict half-Singleton bound, respectively.